

$$2 \cos nx \cos mx = \cos(n+m)x + \cos(n-m)x$$

$$2 \sin nx \sin mx = \cos(n-m)x - \cos(n+m)x$$

$$2 \sin nx \cos mx = \sin(n+m)x + \sin(n-m)x.$$

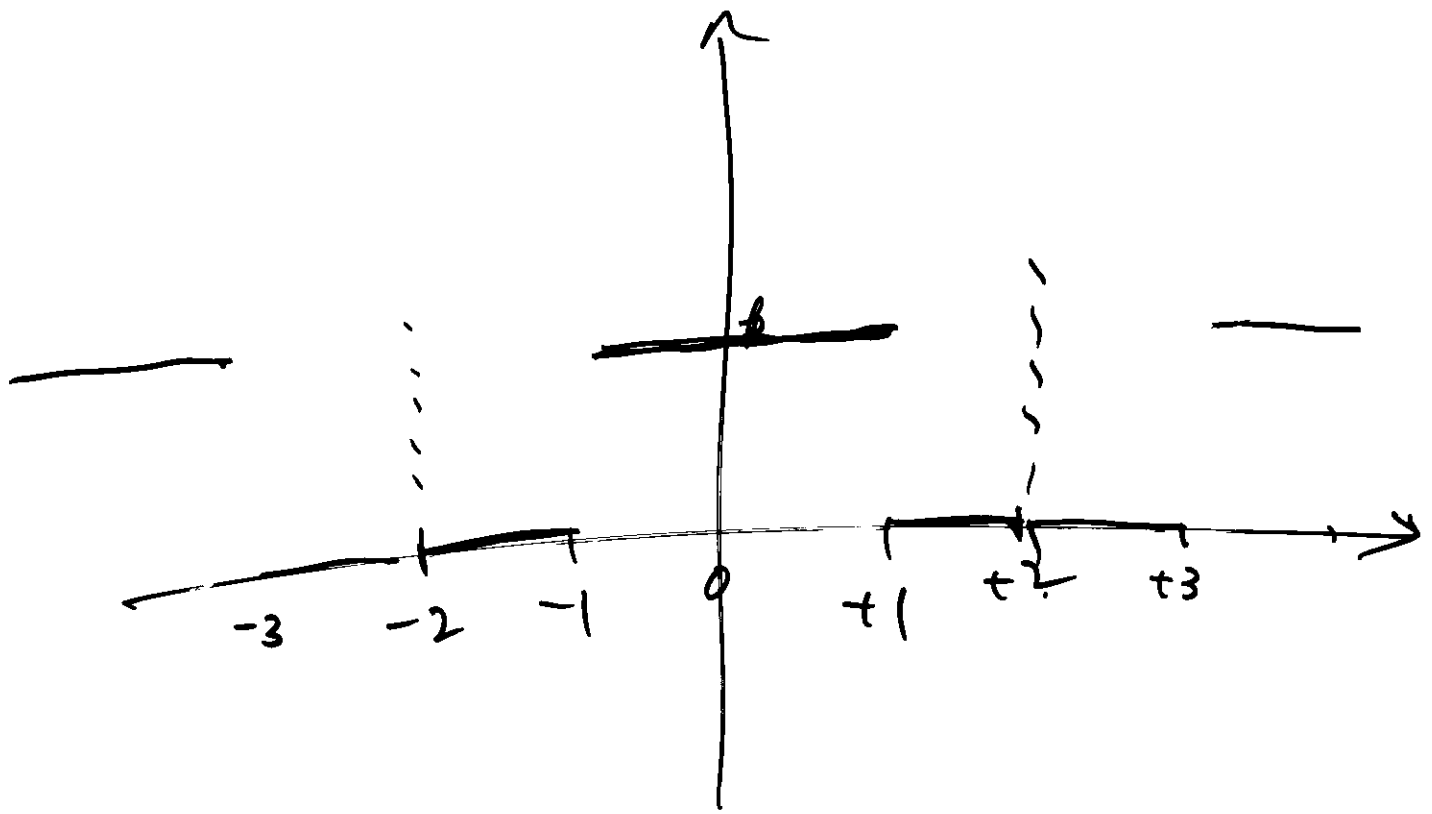
$$e^{i\theta} = \cos \theta + i \sin \theta$$

$$e^{inx} = \cos nx + i \sin nx.$$

$$e^{-inx} = \cos nx - i \sin nx$$

$$\Rightarrow \cos nx = \frac{1}{2} [e^{inx} + e^{-inx}]$$

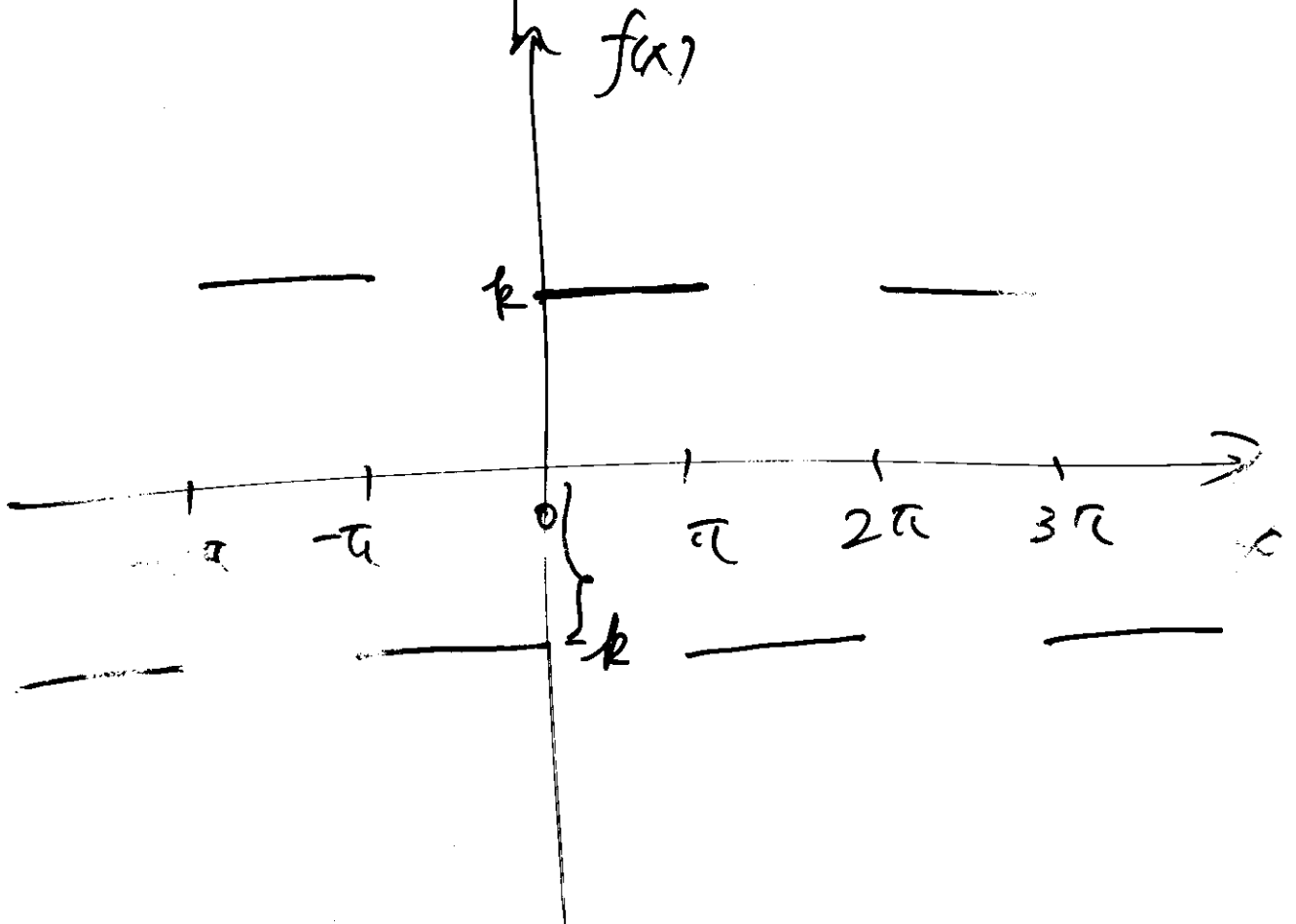
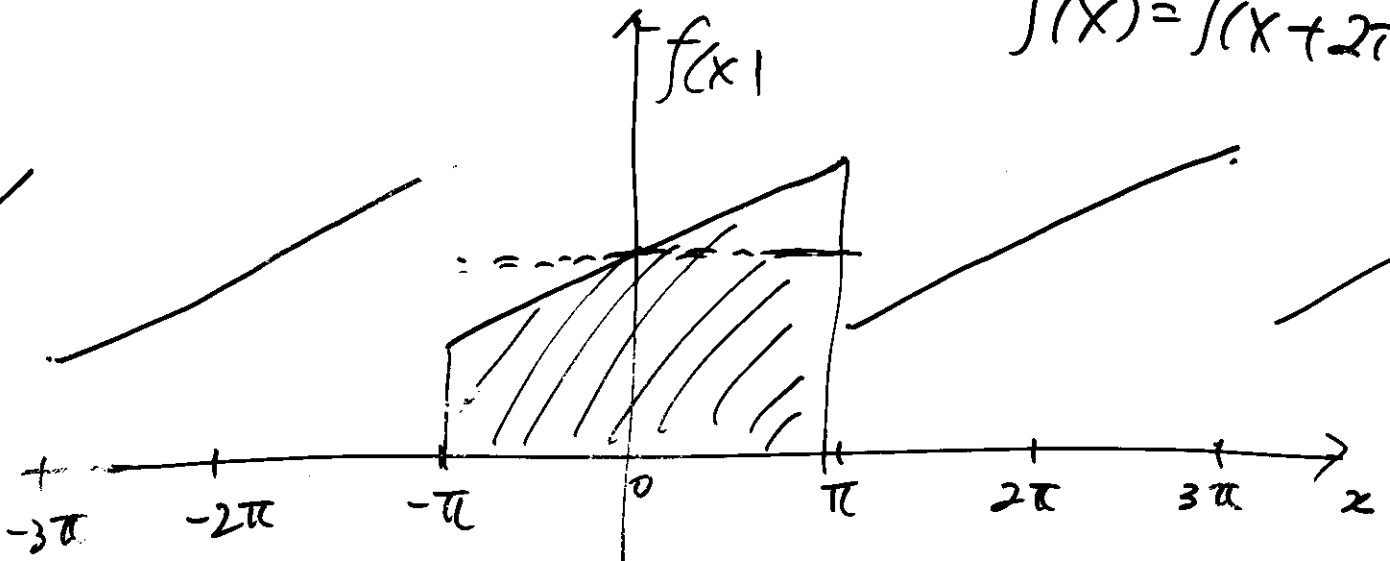
$$\sin nx = \frac{1}{2i} [e^{inx} - e^{-inx}]$$

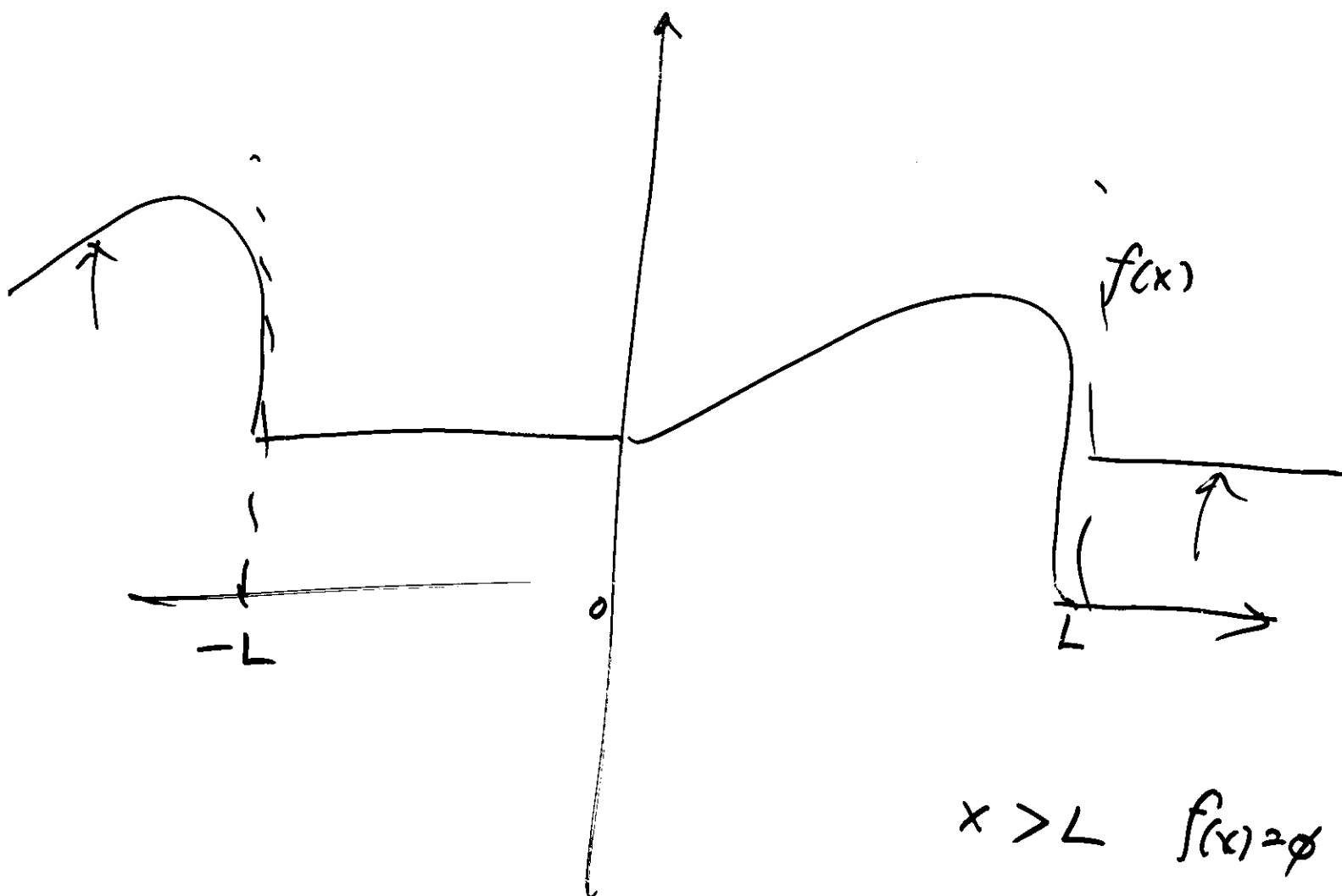


Even: $f(x) = f(-x)$

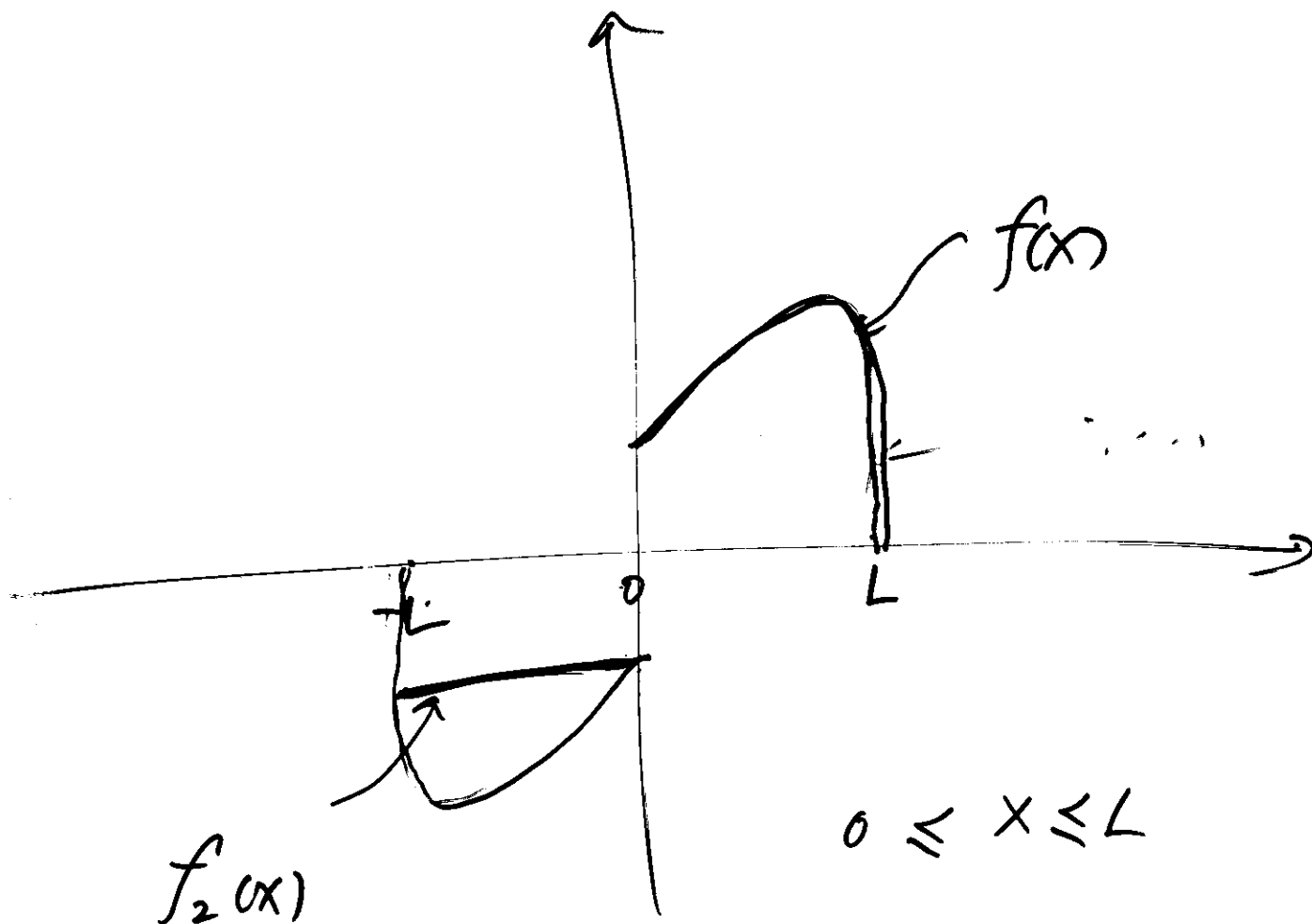
Odd: $f(x) = -f(-x)$

$$f(x) = f(x + 2\pi)$$





$$f(x) = f(x + 2L)$$



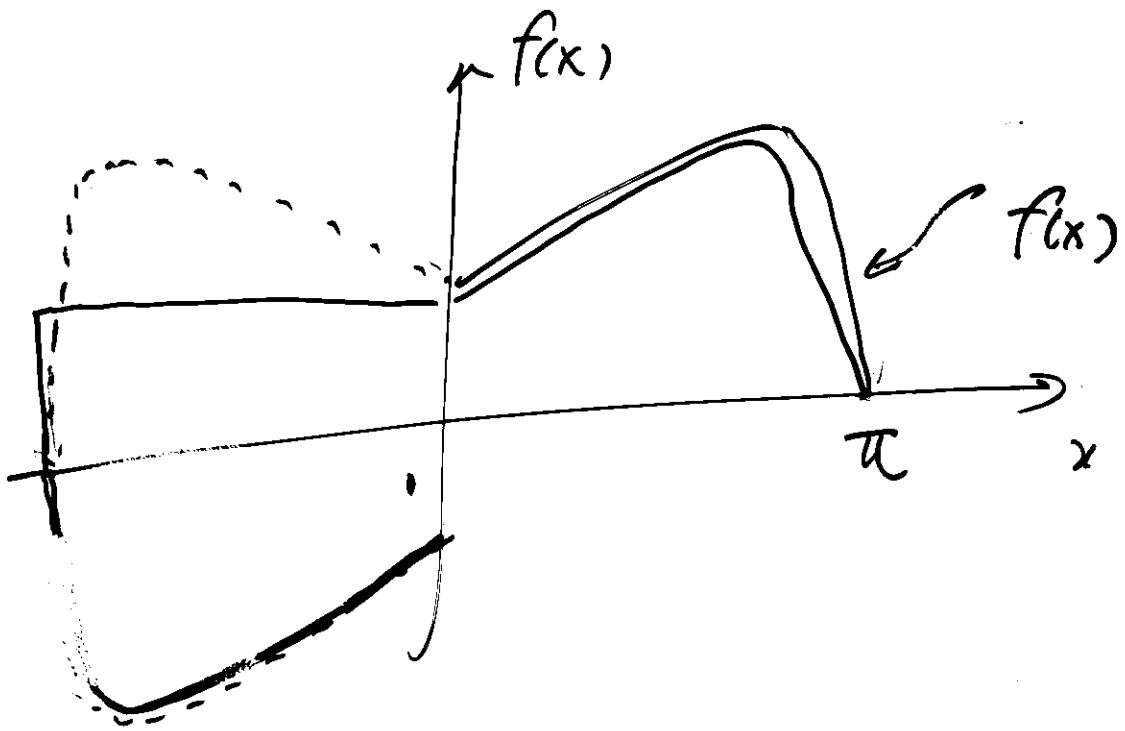
$$f_1(x) = f(x) \quad \text{for } 0 \leq x \leq L$$

$$= -f(-x) \quad \text{for } -L \leq x \leq 0$$

$$f_1(x+2L) = f_1(x)$$

$$= a_0 + \sum_{n=1}^{\infty} a_n \cos \frac{n\pi x}{L} + b_n \sin \frac{n\pi x}{L}$$

$$f_1(x) = \sum_{n=1}^{\infty} b_n \sin \frac{n\pi x}{L}$$



$$f(x) = f(-x)$$

